



MASTER RECURSION



CPMSOC

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Length of Queue?





Recursion

- Decompose the problem into similar sub-problems
- Solve the sub-problems (magically!) using recursion
- Merge the solutions to get the final soln



Recursion



```
1  function length(n) {  
2      // Base Case  
3      if (n == 1) return 1;  
4      // Recurrence Relation  
5      return length(n - 1) + 1;  
6  }
```



Fibonacci!

- Each term of the sequence is defined as the sum of previous 2 terms
- $\text{Fib}(0) = 0, \text{Fib}(1) = 1$
- $\text{Fib}(n) = \text{Fib}(n-1) + \text{Fib}(n-2)$
- 0, 1, 1, 2, 3, 5, 8...

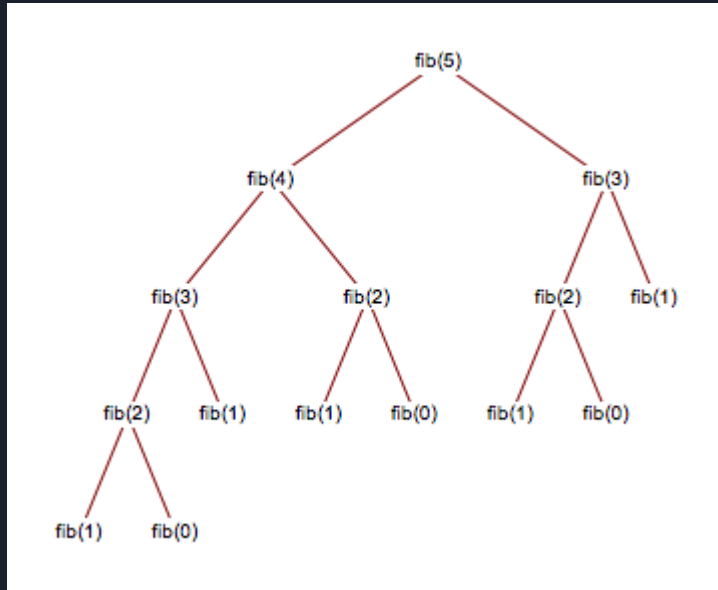


Fibonacci!

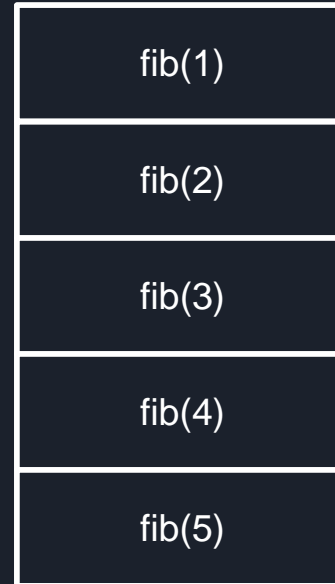


```
1 int fib(int n) {  
2     // Base Cases  
3     if (n == 0) return 0;  
4     if (n == 1) return 1;  
5     // Recurrence Relation  
6     return fib(n - 1) + fib(n - 2);  
7 }
```

Recursion Tree



Recursion Stack





Time & Space Complexity?

→ Time complexity: $O(2^n)$

→ Space complexity: $O(n)$



Exponentiation

- Find a^b using recursion!
- Time complexity: $O(\log(b))$
- Space complexity: $O(\log(b))$



Exponentiation



```
1 int pow(int a, int b) {  
2     if (b == 0) return 1;  
3     int res = pow(a, b / 2);  
4     if (b % 2 == 0) return res * res;  
5     return res * res * a;  
6 }
```



More Recursion!?

- Printing nums from 1 to n
- Factorial
- Sum of node values of a linked list
- Count of a letter in a string
- Subsets of an array



That's all folks!

